

Blokk rejtjelezők

PPKE, ITK

Csapodi Márton

Advanced Encryption Standard

NIST (National Institute of Standards and Technology) kezdeményezésére

Cél: következő évtizedek titkosító algoritmusa a US kormányzat számára

1997. szeptember 12.: Request for candidate algorithms

Minimum feltételek: nyilvános, licenz mentes, szimmetrikus kulcsú, blokk kódoló, blokk méret: 128 bit, kulcs méret: 128/192/256 bit

Értékelési szempontok: biztonság, SW/HW számítási hatékonyság, memóriaszükséglet, rugalmasság (blokk és kulcsméret, számítási platform, konstrukciók: PRNG stb.), egyszerűség

Advanced Encryption Standard

1998. augusztus 20.: 15 First AES Candidates

nyilvános vizsgálat 1999. április 15-ig

1999. augusztus 9.: Round 1 Report (MARS, RC6, Rijndael, Serpent, Twofish)

nyilvános vizsgálat 2000. május 15-ig

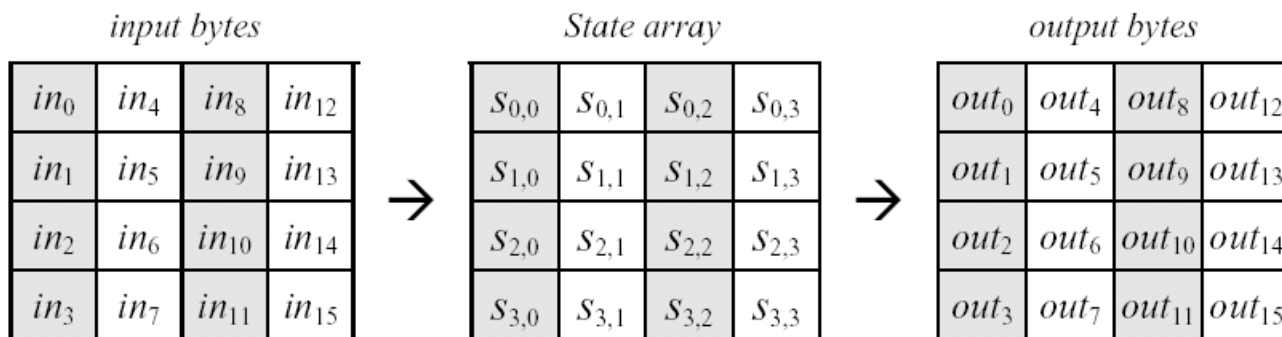
2000. október 2.: Round 2 Report (Rijndael)

FIPS-197: AES Standard, 2001. november 26. (AES-128, AES-192, AES-256)

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128 bites blokk: 16 byte

4x4-es tömbbe rendezve:



a byte-okat polinomként kezeli:

$$b_7x^7 + b_6x^6 + b_5x^5 + b_4x^4 + b_3x^3 + b_2x^2 + b_1x + b_0$$

összeadás, szorzás: $GF(2^8)$ -ben

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AES-ben használt modulus:

$$m(x) = x^8 + x^4 + x^3 + x + 1$$

minden byte reprezentálható polinomként

példa (01010111)x(10000011) szorzásra:

$$\begin{aligned}(x^6 + x^4 + x^2 + x + 1)(x^7 + x + 1) &= x^{13} + x^{11} + x^9 + x^8 + x^7 + \\ &\quad x^7 + x^5 + x^3 + x^2 + x + \\ &\quad x^6 + x^4 + x^2 + x + 1 \\ &= x^{13} + x^{11} + x^9 + x^8 + x^6 + x^5 + x^4 + x^3 + 1\end{aligned}$$

$$\begin{aligned}x^{13} + x^{11} + x^9 + x^8 + x^6 + x^5 + x^4 + x^3 + 1 \text{ modulo } (x^8 + x^4 + x^3 + x + 1) \\ = x^7 + x^6 + 1.\end{aligned}$$

azaz: (01010111)x(10000011)=(11000001) hatékonyan számítható

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4 byte-ból word képezhető: $a(x) = a_3x^3 + a_2x^2 + a_1x + a_0$
az együtthatók $GF(2^8)$ -beliek

összeadás: $a(x) + b(x) = (a_3 \oplus b_3)x^3 + (a_2 \oplus b_2)x^2 + (a_1 \oplus b_1)x + (a_0 \oplus b_0)$

szorzás modulo (x^4+1) : $a(x) \otimes b(x)$

$$d(x) = d_3x^3 + d_2x^2 + d_1x + d_0$$

mátrix alakban:

$$d_0 = (a_0 \bullet b_0) \oplus (a_3 \bullet b_1) \oplus (a_2 \bullet b_2) \oplus (a_1 \bullet b_3)$$

$$d_1 = (a_1 \bullet b_0) \oplus (a_0 \bullet b_1) \oplus (a_3 \bullet b_2) \oplus (a_2 \bullet b_3)$$

$$d_2 = (a_2 \bullet b_0) \oplus (a_1 \bullet b_1) \oplus (a_0 \bullet b_2) \oplus (a_3 \bullet b_3)$$

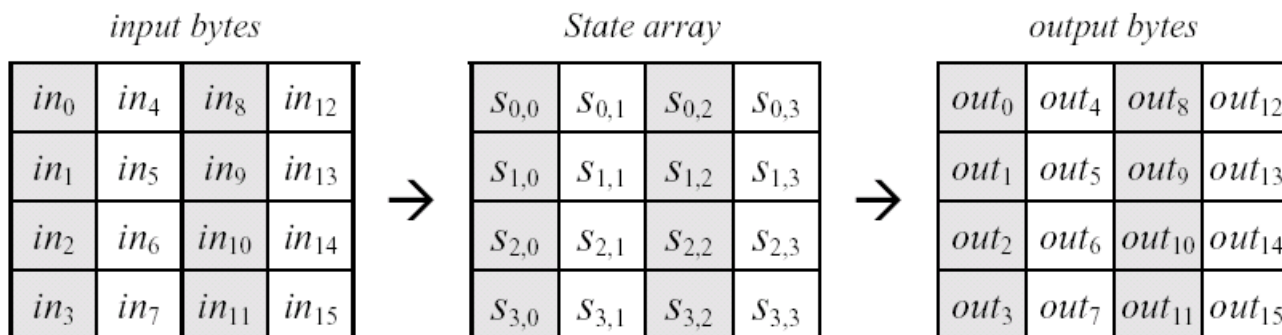
$$d_3 = (a_3 \bullet b_0) \oplus (a_2 \bullet b_1) \oplus (a_1 \bullet b_2) \oplus (a_0 \bullet b_3)$$

$$\begin{bmatrix} d_0 \\ d_1 \\ d_2 \\ d_3 \end{bmatrix} = \begin{bmatrix} a_0 & a_3 & a_2 & a_1 \\ a_1 & a_0 & a_3 & a_2 \\ a_2 & a_1 & a_0 & a_3 \\ a_3 & a_2 & a_1 & a_0 \end{bmatrix} \begin{bmatrix} b_0 \\ b_1 \\ b_2 \\ b_3 \end{bmatrix}$$

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4x4-es tömb oszlopai: egy 32 bites word

oszlopok száma: $N_b=4$



kulcsok: 128/192/256 bit, vagyis 4 soros tömbbe rendezve: $N_k=4, 6$ vagy 8

round: helyettesítés
 sor eltolás
 oszlop keverés
 kulcs hozzáadás

	Key Length (N_k words)	Block Size (N_b words)	Number of Rounds (N_r)
AES-128	4	4	10
AES-192	6	4	12
AES-256	8	4	14

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```
Cipher(byte in[4*Nb], byte out[4*Nb], word w[Nb*(Nr+1)])
begin
    byte state[4,Nb]

    state = in

    AddRoundKey(state, w[0, Nb-1])           // See Sec. 5.1.4

    for round = 1 step 1 to Nr-1
        SubBytes(state)                      // See Sec. 5.1.1
        ShiftRows(state)                    // See Sec. 5.1.2
        MixColumns(state)                   // See Sec. 5.1.3
        AddRoundKey(state, w[round*Nb, (round+1)*Nb-1])
    end for

    SubBytes(state)
    ShiftRows(state)
    AddRoundKey(state, w[Nr*Nb, (Nr+1)*Nb-1])

    out = state
end
```

```
InvCipher(byte in[4*Nb], byte out[4*Nb], word w[Nb*(Nr+1)])
begin
    byte state[4,Nb]

    state = in

    AddRoundKey(state, w[Nr*Nb, (Nr+1)*Nb-1]) // See Sec. 5.1.4

    for round = Nr-1 step -1 downto 1
        InvShiftRows(state)                  // See Sec. 5.3.1
        InvSubBytes(state)                  // See Sec. 5.3.2
        AddRoundKey(state, w[round*Nb, (round+1)*Nb-1])
        InvMixColumns(state)                // See Sec. 5.3.3
    end for

    InvShiftRows(state)
    InvSubBytes(state)
    AddRoundKey(state, w[0, Nb-1])

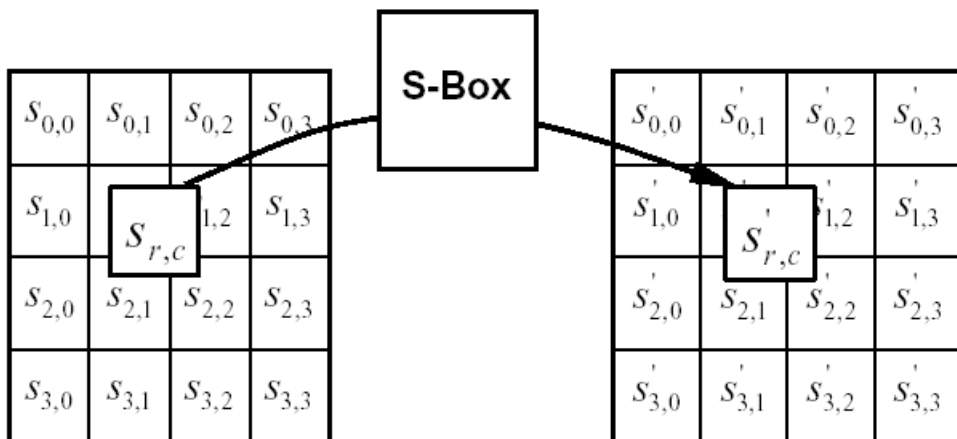
    out = state
end
```

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helyettesítés (SubBytes): inverz GF(2⁸)-ban, majd

leképezés:

$$\begin{bmatrix} b'_0 \\ b'_1 \\ b'_2 \\ b'_3 \\ b'_4 \\ b'_5 \\ b'_6 \\ b'_7 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 \\ 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} b_0 \\ b_1 \\ b_2 \\ b_3 \\ b_4 \\ b_5 \\ b_6 \\ b_7 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 0 \end{bmatrix}$$



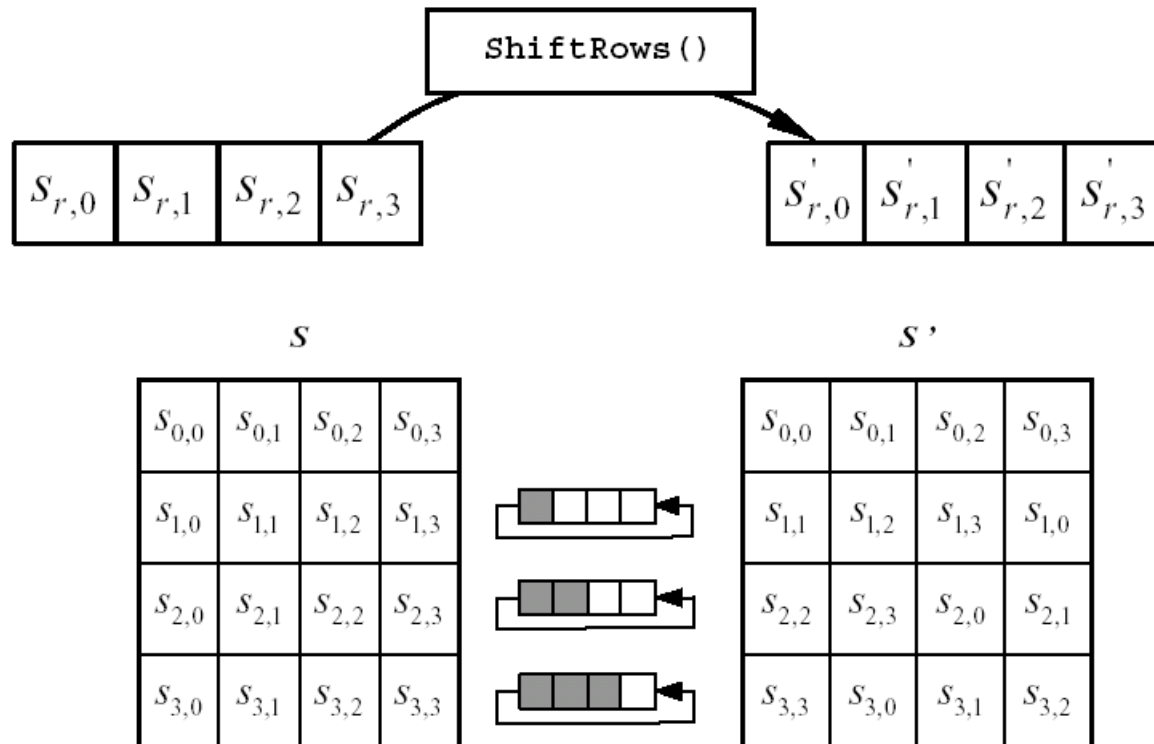
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		y															
		0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
x	0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
	1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
	2	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
	3	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
	4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
	5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
	6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
	7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
	8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
	9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
	a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
	b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
	c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
	d	70	3e	b5	66	48	03	f6									
	e	e1	f8	98	11	69	d9	8e									
	f	8c	a1	89	0d	bf	e6	42									

		y															
		0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
x	0	52	09	6a	d5	30	36	a5	38	bf	40	a3	9e	81	f3	d7	fb
	1	7c	e3	39	82	9b	2f	ff	87	34	8e	43	44	c4	de	e9	cb
	2	54	7b	94	32	a6	c2	23	3d	ee	4c	95	0b	42	fa	c3	4e
	3	08	2e	a1	66	28	d9	24	b2	76	5b	a2	49	6d	8b	d1	25
	4	72	f8	f6	64	86	68	98	16	d4	a4	5c	cc	5d	65	b6	92
	5	6c	70	48	50	fd	ed	b9	da	5e	15	46	57	a7	8d	9d	84
	6	90	d8	ab	00	8c	bc	d3	0a	f7	e4	58	05	b8	b3	45	06
	7	d0	2c	1e	8f	ca	3f	0f	02	c1	af	bd	03	01	13	8a	6b
	8	3a	91	11	41	4f	67	dc	ea	97	f2	cf	ce	f0	b4	e6	73
	9	96	ac	74	22	e7	ad	35	85	e2	f9	37	e8	1c	75	df	6e
	a	47	f1	1a	71	1d	29	c5	89	6f	b7	62	0e	aa	18	be	1b
	b	fc	56	3e	4b	c6	d2	79	20	9a	db	c0	fe	78	cd	5a	f4
	c	1f	dd	a8	33	88	07	c7	31	b1	12	10	59	27	80	ec	5f
	d	60	51	7f	a9	19	b5	4a	0d	2d	e5	7a	9f	93	c9	9c	ef
	e	a0	e0	3b	4d	ae	2a	f5	b0	c8	eb	bb	3c	83	53	99	61
	f	17	2b	04	7e	ba	77	d6	26	e1	69	14	63	55	21	0c	7d

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sor eltolás (ShiftRows):



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oszlop keverés (MixColumns):

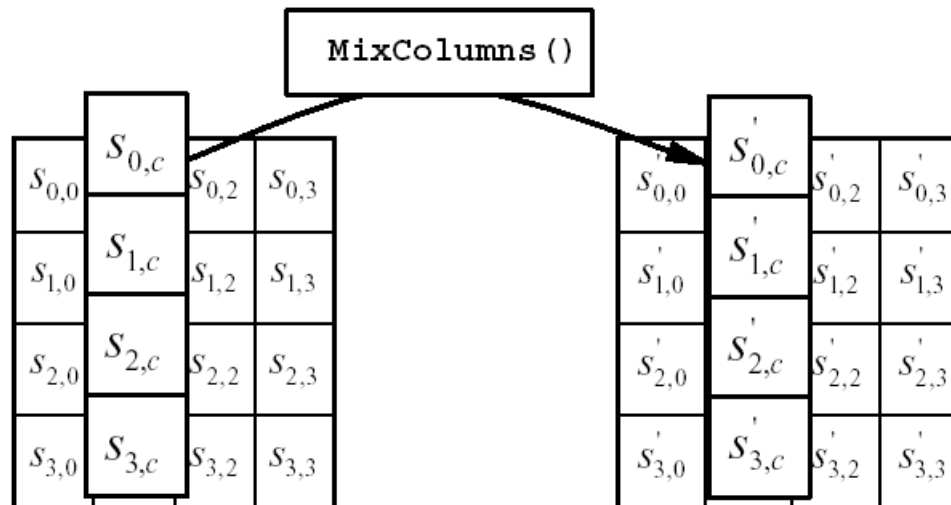
az oszlop polinom szorzása

$$s'(x) = a(x) \otimes s(x)$$

$$a(x) = \{03\}x^3 + \{01\}x^2 + \{01\}x + \{02\}$$

$$a^{-1}(x) = \{0b\}x^3 + \{0d\}x^2 + \{09\}x + \{0e\}$$

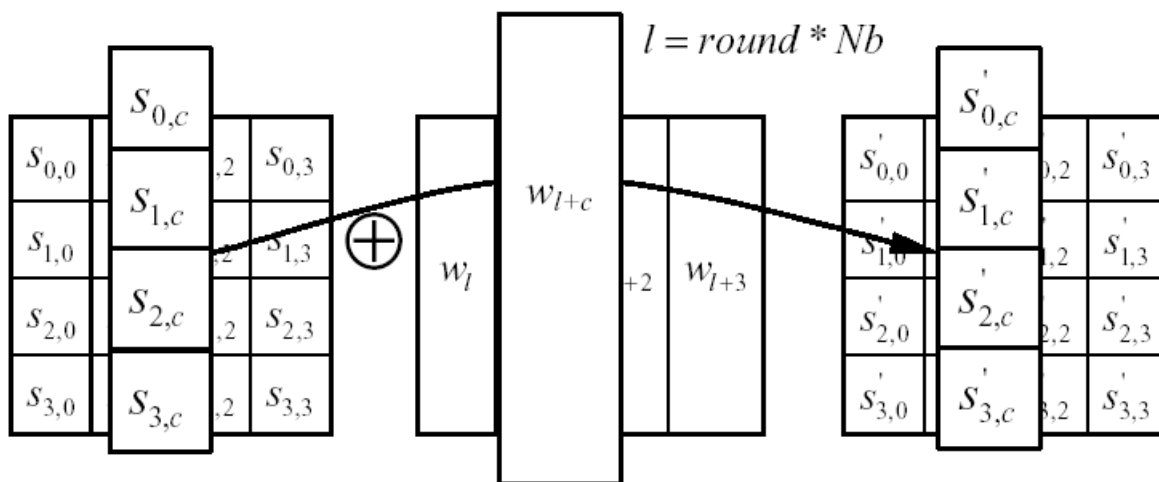
$$\begin{bmatrix} s'_{0,c} \\ s'_{1,c} \\ s'_{2,c} \\ s'_{3,c} \end{bmatrix} = \begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \begin{bmatrix} s_{0,c} \\ s_{1,c} \\ s_{2,c} \\ s_{3,c} \end{bmatrix}$$



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kulcs hozzáadás (AddRoundKey):

$$[S'_{0,c}, S'_{1,c}, S'_{2,c}, S'_{3,c}] = [S_{0,c}, S_{1,c}, S_{2,c}, S_{3,c}] \oplus [w_{round * Nb + c}]$$



$Nb(Nr+1)$ 4 byte-os kulcsot képez az $Nk \times 4$ byte-os kulcsból

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kulcs kiterjesztés (Key Expansion):

```
KeyExpansion(byte key[4*Nk], word w[Nb*(Nr+1)], Nk)
begin
    word temp

    i = 0

    while (i < Nk)
        w[i] = word(key[4*i], key[4*i+1], key[4*i+2], key[4*i+3])
        i = i+1
    end while

    i = Nk

    while (i < Nb * (Nr+1))
        temp = w[i-1]
        if (i mod Nk = 0)
            temp = SubWord(RotWord(temp)) xor Rcon[i/Nk]
        else if (Nk > 6 and i mod Nk = 4)
            temp = SubWord(temp)
        end if
        w[i] = w[i-Nk] xor temp
        i = i + 1
    end while
end
```

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Cipher Key = 2b 7e 15 16 28 ae d2 a6 ab f7 15 88 09 cf 4f 3c

$w_0 = 2b7e1516$

$w_1 = 28aed2a6$

$w_2 = abf71588$

$w_3 = 09cf4f3c$

i (dec)	temp	After RotWord()	After SubWord()	Rcon[i/Nk]	After XOR with Rcon	w[i-Nk]	w[i] = temp XOR w[i-Nk]
4	09cf4f3c	cf4f3c09	8a84eb01	01000000	8b84eb01	2b7e1516	a0fafe17
5	a0fafe17					28aed2a6	88542cb1
6	88542cb1					abf71588	23a33939
7	23a33939					09cf4f3c	2a6c7605
8	2a6c7605	6c76052a	50386be5	02000000	52386be5	a0fafe17	f2c295f2
9	f2c295f2					88542cb1	7a96b943
10	7a96b943					23a33939	5935807a
11	5935807a					2a6c7605	7359f67f
12	7359f67f	59f67f73	cb42d28f	04000000	cf42d28f	f2c295f2	3d80477d
13	3d80477d					7a96b943	4716fe3e
14	4716fe3e					5935807a	1e237e44

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Input = 32 43 f6 a8 88 5a 30 8d 31 31 98 a2 e0 37 07 34

Cipher Key = 2b 7e 15 16 28 ae d2 a6 ab f7 15 88 09 cf 4f 3c

Round Number	Start of Round	After SubBytes	After ShiftRows	After MixColumns	Round Key Value																																																																																
input	<table><tr><td>32</td><td>88</td><td>31</td><td>e0</td></tr><tr><td>43</td><td>5a</td><td>31</td><td>37</td></tr><tr><td>f6</td><td>30</td><td>98</td><td>07</td></tr><tr><td>a8</td><td>8d</td><td>a2</td><td>34</td></tr></table>	32	88	31	e0	43	5a	31	37	f6	30	98	07	a8	8d	a2	34	<table><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr></table>																	<table><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr></table>																	<table><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr></table>																	<table><tr><td>2b</td><td>28</td><td>ab</td><td>09</td></tr><tr><td>7e</td><td>ae</td><td>f7</td><td>cf</td></tr><tr><td>15</td><td>d2</td><td>15</td><td>4f</td></tr><tr><td>16</td><td>a6</td><td>88</td><td>3c</td></tr></table> ⊕ =	2b	28	ab	09	7e	ae	f7	cf	15	d2	15	4f	16	a6	88	3c
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	19	a0	9a	e9																																																																																	
	3d	f4	c6	f8																																																																																	
	e3	e2	8d	48																																																																																	
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